

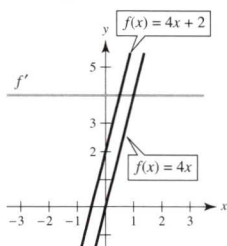
Chapter 4

Section 4.1 (page 255)

- 1-3. Proofs 5. $y = 3t^3 + C$ 7. $y = \frac{2}{5}x^{5/2} + C$
- | Original Integral | Rewrite | Integrate | Simplify |
|-----------------------------------|------------------------------|--|---------------------------|
| 9. $\int \sqrt[3]{x} dx$ | $\int x^{1/3} dx$ | $\frac{x^{4/3}}{4/3} + C$ | $\frac{3}{4}x^{4/3} + C$ |
| 11. $\int \frac{1}{x\sqrt{x}} dx$ | $\int x^{-3/2} dx$ | $\frac{x^{-1/2}}{-1/2} + C$ | $-\frac{2}{\sqrt{x}} + C$ |
| 13. $\int \frac{1}{2x^3} dx$ | $\frac{1}{2} \int x^{-3} dx$ | $\frac{1}{2} \left(\frac{x^{-2}}{-2} \right) + C$ | $-\frac{1}{4x^2} + C$ |
15. $\frac{1}{2}x^2 + 7x + C$ 17. $x^2 - x^3 + C$ 19. $\frac{1}{6}x^6 + x + C$
 21. $\frac{2}{5}x^{5/2} + x^2 + x + C$ 23. $\frac{3}{5}x^{5/3} + C$ 25. $-1/(4x^4) + C$
 27. $\frac{2}{3}x^{3/2} + 12x^{1/2} + C = \frac{2}{3}x^{1/2}(x + 18) + C$
 29. $x^3 + \frac{1}{2}x^2 - 2x + C$
 31. $\frac{2}{7}y^{7/2} + C$ 33. $x + C$ 35. $5 \sin x - 4 \cos x + C$
 37. $t + \csc t + C$ 39. $\tan \theta + \cos \theta + C$ 41. $\tan y + C$
 43. $-\csc x + C$

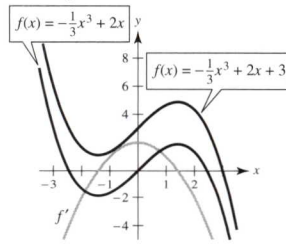
45. Answers will vary.

Example:



47. Answers will vary.

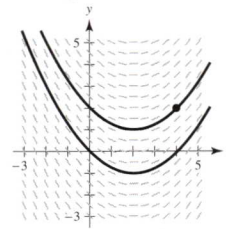
Example:



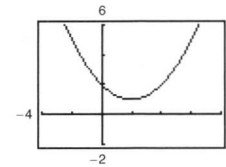
49. $y = x^2 - x + 1$

51. (a) Answers will vary.

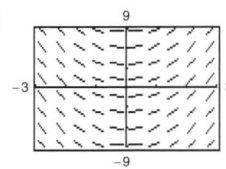
Example:



(b) $y = \frac{1}{4}x^2 - x + 2$

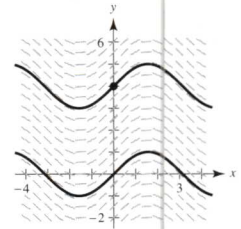


55. (a)

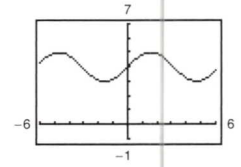


53. (a) Answers will vary.

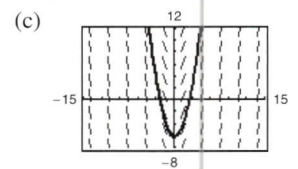
Example:



(b) $y = \sin x + 4$



(b) $y = x^2 - 6$



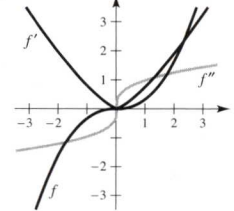
57. $f(x) = 3x^2 + 8$ 59. $h(t) = 2t^4 + 5t - 11$

61. $f(x) = x^2 + x + 4$ 63. $f(x) = -4\sqrt{x} + 3x$

65. (a) $h(t) = \frac{3}{4}t^2 + 5t + 12$ (b) 69 cm

67. When you evaluate the integral $\int f(x) dx$, you are finding a function $F(x)$ that is an antiderivative of $f(x)$. So, there is no difference.

69.



71. 62.25 ft 73. $v_0 \approx 187.617$ ft/sec

75. $v(t) = -9.8t + C_1 = -9.8t + v_0$
 $f(t) = -4.9t^2 + v_0t + C_2 = -4.9t^2 + v_0t + s_0$

77. 7.1 m 79. 320 m; -32 m/sec

81. (a) $v(t) = 3t^2 - 12t + 9$; $a(t) = 6t - 12$

(b) (0, 1), (3, 5) (c) -3

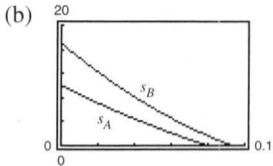
83. $a(t) = -1/(2t^{3/2})$; $x(t) = 2\sqrt{t} + 2$

85. (a) 1.18 m/sec² (b) 190 m

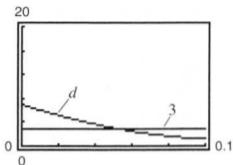
87. (a) 300 ft (b) 60 ft/sec ≈ 41 mi/h

89. (a) Airplane A: $s_A = \frac{625}{2}t^2 - 150t + 10$

Airplane B: $s_B = \frac{49,275}{68}t^2 - 250t + 17$



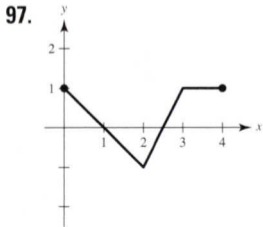
(c)
$$d = \frac{28,025}{68}t^2 - 100t + 7$$



Yes, $d < 3$ for $t > 0.0505$ h

91. True 93. True

95. False. f has an infinite number of antiderivatives, each differing by a constant.



99. Proof